

TOPICS		Content	Guidance	R	A	G
Algebra & Functions	2.1	Index laws	$\sqrt{2}$ is irrational			
	2.2	surds	including rationalising the denominator			
	2.3	Quadratic functions & their graphs	f(x) notation			
		Discriminant	including conditions for number of real roots			
		Completing the square	including coef of x not equal to 1			
		solution of quadratic equations	factorising			
			formula			
			completing the square			
		solving quadratic equations in a function of the unknown	powers of x, trig functions, e & log functions (where you can put it equal to a different letter to make a normal quadratic)			
	2.4	simultaneous equations	elimination or substitution			
			including one linear & one quadratic			
	2.5	linear & quadratic inequalities & interpret graphically	including $px^2 + qx + r > ax + b$			
			means where the curve is above the line etc			
		including inequalities with brackets & fractions	eg need to be rearranged first into solvable form			
	express solutions through correct use of 'and' & 'or'	ie set notation				
	graphs of inequalities	shading & use of dotted & solid lines to find solution set				

	<b>2.6</b>	<b>manipulating polynomials , algebraic division &amp; use of factor theorem</b>	including factorising a cubic			
		<b>simplify rational expressions by factorising &amp; cancelling &amp; algebraic division</b>	ie algebraic fractions			
	<b>2.7</b>	<b>Graphs of functions; sketch curves</b>	cubic & quartic functions			
		<b>modulus functions</b>	sketch modulus functions & use to solve equations & inequalities			
		$\frac{a}{x}$ & $\frac{a}{x^2}$	asymptotes			
		<b>interpret solutions of equations in relation to graphs &amp; points of in</b>				
		<b>proprtional relationships &amp; their graphs</b>	$y \propto x$ or $\frac{1}{x}$ or $=kx$ etc			
	<b>2.8</b>	<b>composite funtions, inverse functions &amp; their graphs</b>	function is one-to-one or many-to-one, f: I → domain & range			
	<b>2.9</b>	<b>transforming graphs &amp; sketching</b>	apply a combination of transformations to any graphs on the syllabus (quadratic, cubic, sin, tan, cos, $e^x$ & $a^x$ )			
	<b>.2.10</b>	<b>partial fractions</b>	& apply to integration, differentiation, & series expansion			
	<b>2.11</b>	<b>modelling</b>	eg trig functions - tides/hours of sunlight, reciprocal for inverse propportion, exponential for growth & decay			
<b>Coordinate Geometry</b>	<b>3.1</b>	<b>straight line equations</b>				
		<b>gradient conditions of parallel &amp; perpendicular lines</b>				
		<b>straight lines in context</b>				
	<b>3.2</b>	<b>equation of a circle</b>	find raduis & centre (in either form)			
		<b>complete the square to find centre &amp; radius</b>				
		<b>circle properties:</b>				
		<b>angle in a semicircle</b>	find equation of circumcircle given 3 points			
		<b>radius bisects chord at right angles</b>				
		<b>tangent is perpendicular to radius</b>	equation of a tangent using this			
	<b>3.3</b>	<b>parametric equations &amp; conversion between Cartesian &amp; parametric forms</b>	pay attention to the domain of t			
	<b>3.4</b>	<b>use parametrics in modelling</b>	including constant velocity as in kinematics			

Sequences & Series	4.1	binomial for positive integer power, n!	pascal's triangle, notations $\binom{n}{r}$ & $nC_r$			
		any rational power & valid for $ r  < 1$	may be used with partial fractions & may be asked about validity of expansion			
	4.2	sequences including an nth term rule, increasing, decreasing & periodic functions	eg: $U_n = \frac{1}{3n+1}$ is decreasing as $U_{n+1} < U_n$ for all n $U_n = 2^n$ is increasing as $U_{n+1} > U_n$ etc			
	4.3	sigma notation	know that $\sum_1^n 1 = n$			
	4.4	arithmetic sequences & series	proof of sum formula, including sum of first n natural numbers			
	4.5	geometric sequences & series	proof of sum formula, use of logs, sum to infinity of convergent series & condition $ r  < 1$			
	4.6	use in modelling	eg savings scheme (percentage increase forms geometric series)			
Trigonometry	5.1	sin, cos, tan	unit circle			
		sine & cosine rules	including ambiguous case of sine rule			
		area of triangle				
		radians, including arc length & area of sector				
	5.2	small angle approximations	$\frac{\cos 3x - 1}{x \sin 4x} \approx -\frac{9}{8}$			
5.3	trig graphs (symmetry & periodicity)					
		exact values of sin/cos/tan of $0, \frac{\pi}{6}, \frac{\pi}{4}, \frac{\pi}{3}, \frac{\pi}{2}, \pi$				
	5.4	sec cosec & cot, arcsin arccos & arctan; their graphs, ranges & domains	angles in degrees & radians			
	5.5	$\tan \theta = \frac{\sin \theta}{\cos \theta}$	use to solve equations & prove further identities in both degrees & radians			
		$\sin^2 \theta + \cos^2 \theta = 1,$ $1 + \tan^2 \theta = \sec^2 \theta,$ $1 + \cot^2 \theta = \text{cosec}^2 \theta$				

	5.6	double angle formulae & sin/tan/cos (A+B) & (A-B) geometric proofs of these  $r \sin(\theta \pm \alpha)$ & $r \cos(\theta \pm \alpha)$	apply to half angles  solve equations like $a \cos \theta + b \sin \theta = c$			
	5.7	solve trig equations including quadratics & multiples of the angle				
	5.8	proofs of identities				
	5.9	solve problems in context including vectors, kinematics & forces				
Exponentials & logs	6.1	know & use $a^x, e^x$	& their graphs. Understand difference in shape between $a < 1$ & $a > 1$			
	6.2	know that the gradient of $e^{kx}$ is $ke^{kx}$	When the rate of change is proportional to $y$ , an exponential model should be used			
	6.3	know $\log_a x$ is the inverse of $a^x$				
		$\ln x$	solve equations like $e^{ax+b} = p$ & $\ln(ax + b) = q$			
	6.4	log laws				
	6.5	solve equations in the form $a^x=b$				
	6.6	reduce exponentials to linear relations	plot $\log y$ against $\log x$ & $\log y$ against $x$ . & find gradient & intercept of line			
	6.7	growth & decay	know that "initial" means $t=0$			
Differentiation	7.1	understand the derivative as the gradient of the tangent at a general point (x,y), as a limit & as a rate of change sketch the gradient function  second derivatives differentiation from first principles convex & concave sections of curve & points of inflection	given $y=f(x)$ , sketch $y=f'(x)$ . Can also relate to speed & acceleration  for powers of $x$ & for sin & cos (use formula) know that stationary points are where $f'(x)=0$ , that point of inflection is $f''(x)$ changes sign & use second derivatives for nature of maximum & minimum points			
		7.2	differentiate $x^n$	put in index form first if necessary		

		differentiate $a^x, e^x, \sin kx$ $\cos kx, \tan kx, \ln x$			
	<b>7.3</b>	apply differentiation to to find gradients, tangents & normals			
		max & min & points of inflection	max & min problems in context		
		increasing & decreasing functions	apply to curve sketching		
	<b>7.4</b>	product , quotient & chain rules, including connected rates of change & inverse functions	cosec, cotan & sec		
			use $\frac{dy}{dx} = \frac{1}{\frac{dx}{dy}}$ & $\frac{dV}{dt} = \frac{dV}{dr} \times \frac{dr}{dt}$		
	<b>7.5</b>	implicit & parametric	equations of tangents & normals of curves given parametrically or implicitly		
	<b>7.6</b>	construct simple differential equations in pure maths & in context	info given may include direct proportion		
<b>Integration</b>	<b>8.1</b>	integration as reverse of differentiation	constant of integration		
	<b>8.2</b>	integrate $x^n, e^{kx}, \frac{1}{x}, \sin x, \cos x$	put in index form first if necessary  given f'(x) and a point on the curve, find an equation of the curve  include other standard trig functions & use identities to integrate $\sin^2 \cos^2 \tan^2$		
	<b>8.3</b>	areas under curves			
		areas between 2 curves			
	<b>8.4</b>	integration as a limit	$\int_a^b f(x)dx = \lim_{\delta x \rightarrow 0} \sum_{x=a}^b f(x)\delta x$		
	<b>8.5</b>	integration by substitution	includes finding suitable substitution		
		integration by parts			
		inverse chain rule			
	<b>8.6</b>	integration using partial fractioning			
	<b>8.7</b>	differential equations	may need to sketch family of curves		

	<b>8.8</b>	<b>interpret solutions of differential equations in context</b>	includes links to kinematics (variable acceleration) & limitations on the model			
<b>Numerical methods</b>	<b>9.1</b>	<b>find roots of <math>f(x)=0</math> by considering changes of sign</b>	know that function has to be continuous			
		<b>understand how it can fail</b>				
	<b>9.2</b>	<b>iteration</b>	cobweb & staircase			
	<b>9.3</b>	<b>Newton-Raphson</b>	understand how it works geometrically; fails if near turning points			
	<b>9.4</b>	<b>trapezium rule</b>	use a sketch to determine over/under-estimate			
			$\vec{AB} = \mathbf{b} - \mathbf{a}$			